

Towards understanding QCD phase diagram from the fluctuations of conserved charges

Sayantan Sharma



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Bielefeld-BNL-CCNU collaboration

A. Bazavov, H.-T. Ding, P. Hegde, O. Kaczmarek, F. Karsch, E. Laermann, S. Mukherjee, H. Ohno, P. Petreczky, C. Schmidt, S. Sharma, W. Soeldner, P. Steinbrecher, M. Wagner

Outline

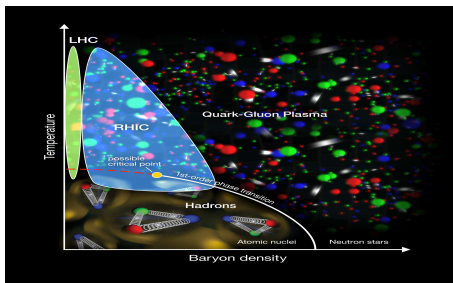
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- 2 Fluctuations and the physics near chiral crossover transition
- 3 QCD medium for $T > T_c$

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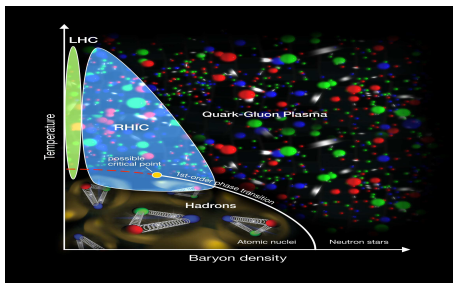
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[<http://www.bnl.gov/rhic/news>]

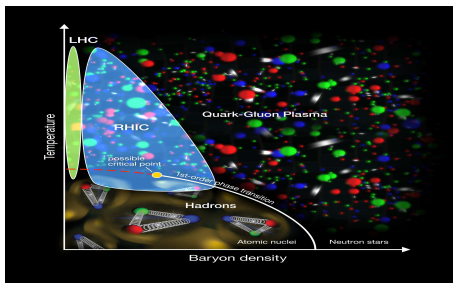
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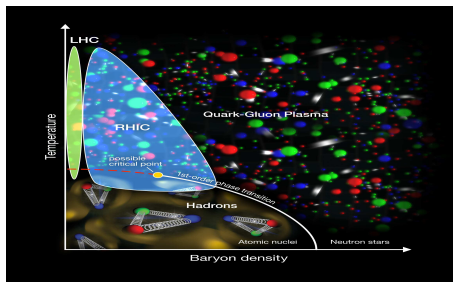
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- What are the degrees of freedom of QCD at finite temperature and the interactions between them?
- How reliably can weak coupling perturbative calculations describe the QGP?
- Lattice calculations also provide a baseline for the observations of fluctuations of conserved charges from Heavy Ion collision experiments.



Basic observables: Fluctuations of conserved charges

- Measure the fluctuations of conserved charges in a Grand Canonical ensemble

$$\chi_{ij}^{XY} = \frac{\partial^{i+j}}{\partial \hat{\mu}_i^X \partial \hat{\mu}_j^Y} P_{QCD}(\mu_x, T) / T^4, \quad \chi_i^X = \frac{\partial^i}{\partial \hat{\mu}_i^X} P_{QCD}(\mu_x, T) / T^4$$

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- The derivatives of pressure can be written in terms of trace of D and its derivatives: Like: $\chi_2^u = \langle \text{Tr}[D^{-1}D'' - D^{-1}D'D^{-1}D'] \rangle + \langle \text{Tr}[D^{-1}D']^2 \rangle$.

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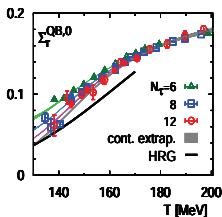
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- No. inversions increases for higher fluctuations \rightarrow numerically expensive. Techniques developed like analytic continuation from imaginary chemical potential data [S. Borsanyi, 15] and recent advances in programming [P. Steinbrecher's, Kate Clark's Talk] to address these issues.

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The fluctuations near T_c

- Ratios of fluctuations $\Sigma_r^{QB} = 0.4 \frac{\chi_2^B}{\chi_2^Q}$ are the simplest to compute.
- Even these simple observables already show a deviation from Hadron Resonance Gas (HRG) Model at $T > 140$ MeV. [Bielefeld-BNL collaboration, 15]



Is Hadron Resonance Gas a good approximation for QCD below T_c ?

- When there are no inelastic collisions \Rightarrow the ensemble can be described by a gas of all measured hadrons and possible resonances (HRG) [Dashen, Ma and Bernstein, 69,71]

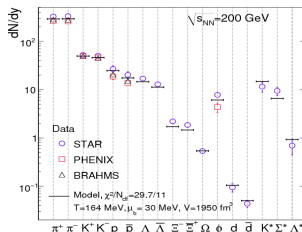
$$\ln \mathcal{Z} = \pm \sum_i g_i \frac{V}{2\pi^2} \int_0^\infty dp p^2 \ln \left(1 \pm e^{\beta(\epsilon_i - \mu_i)} \right),$$

$$\epsilon_i = \sqrt{p^2 + m_i^2} \simeq m_i \quad \& \quad \mu_i = \mu_B B_i + \mu_S S_i + \mu_C C_i + \mu_I I_i.$$

- Residual interactions $\propto n_i n_j \sim e^{-(m_i+m_j)/T}$ suppressed.
 - A virial expansion can be used to estimate the effect of interactions.
 - Scattering phase shifts from expt used to calculate interaction cross-section.
 - HRG a good approximation if resonances very near to two particle threshold.
- [Prakash & Venugopalan, 92]
- For light hadrons validity of HRG needs to be checked! For charm it is expected to work.

HRG and Freezeout data from experiments

- Chemical freezeout \Rightarrow the hadrons do not scatter inelastically.
- Compare the ratio of particle yields from theory and experiments and perform a χ^2 minimization in the $T - \mu_B$ plane.
- If indeed a thermalized medium is formed \Rightarrow get T^f and μ_B^f corresponding to the collision energy of two heavy nuclei.
- **Caveats:** Issues about thermalization, expanding system, momentum cut etc..



Freezeout curve for a thermalized medium

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- Expanding the observable about the freezeout surface at $\mu_B = 0$,
$$\Sigma_r^{QB} = \Sigma_r^{QB}(0) + \left[\Sigma_r^{QB,2} - \kappa_2^f T_{f,0} \frac{d\Sigma_r^{QB,0}}{dT} \Big|_{T_{f,0}} \right] \frac{\mu_B^2}{T^2}.$$

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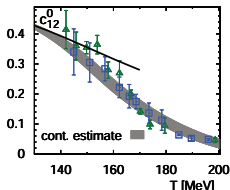
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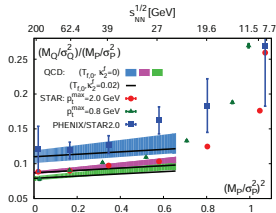
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- An estimate of Σ_r^{QB} and R_{12}^B from experiments allows us to calculate c_{12} . [Bielefeld-BNL collaboration, 15]

- **Caveat:** In experiments one measures protons Σ_r^{QP} , R_{12}^P .
- Additionally take into account also corrections due to finite range of momenta of detected particles [Karsch, Morita and Redlich, 15].
- From the 2 independent expressions of Σ_r^{QB} we extract $c_{12}(T_{f,0}, \kappa_2^f) = c_{12}(T_{f,0}) - \kappa_2^f D_{12}$.





- This exercise give $T_{f,0} = 147$ MeV consistent with expectation that its at or below T_c .

Curvature: $\kappa_2^f < -0.012(15) \rightarrow$ near to chiral curvature $\kappa_2^B = 0.007$.

When do the open-charm hadrons melt

- We want to understand when heavy quarks deconfine looking at the properties of **heavy-light hadrons**.
- The analysis of bound states through the study of spectral functions difficult on the lattice.
- If the charm hadron ensemble near the freezeout well described as a **hadron resonance gas** characterized by T, μ_B, μ_C ,

$$\begin{aligned} P(\hat{\mu}_C, \hat{\mu}_B) &= P_M \cosh(\hat{\mu}_C) + P_{B,C=1} \cosh(\hat{\mu}_B + \hat{\mu}_C) \\ &+ P_{B,C=2} \cosh(\hat{\mu}_B + 2\hat{\mu}_C) + P_{B,C=3} \cosh(\hat{\mu}_B + 3\hat{\mu}_C) . \end{aligned}$$

- The ground state $m_{C=2} - m_{C=1} = 1$ GeV : effect on thermodynamics of $C = 2, 3$ baryons is negligible.

- It is comparatively easy to calculate the fluctuations + correlations of B, C

$$\chi_{ij}^{BC} = \frac{\partial^{i+j}}{\partial \hat{\mu}_i^B \partial \hat{\mu}_j^C} P_{\text{tot}} / T^4$$

- The partial pressures can be constructed out of χ_2^C, χ_{11}^{BC} and $\chi_4^C, \chi_{31}^{BC}, \chi_{22}^{BC}, \chi_{13}^{BC}$. [Bielefeld-BNL collaboration, 13]

- Setting $\mu = 0$ one can rewrite the partial pressures in terms of these quantities like

$$P_M = \chi_2^C - \chi_{22}^{BC}, P_{B,C=1} \sim \chi_{mn}^{BC}, m+n=4$$

A first glimpse at the charm baryons

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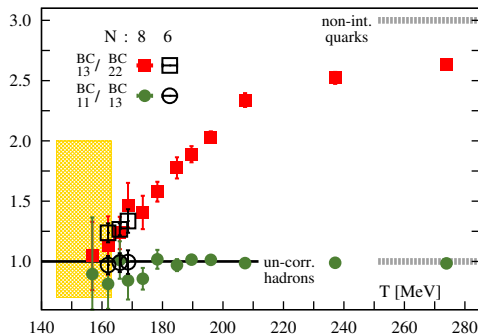
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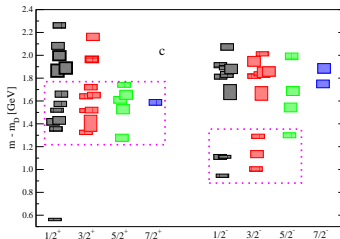
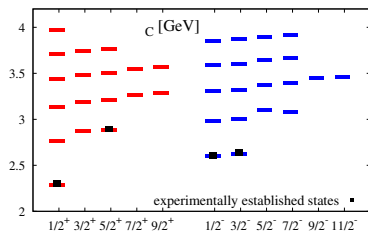
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- Our “order parameter” : $\chi_{13}^{BC} / \chi_{22}^{BC} \rightarrow$ independent of cut-off effects.
- Baryons with charm and light degrees of freedom **melt at T_c** independent of the details of the hadron spectrum. [Bielefeld-BNL collaboration, PLB 14]



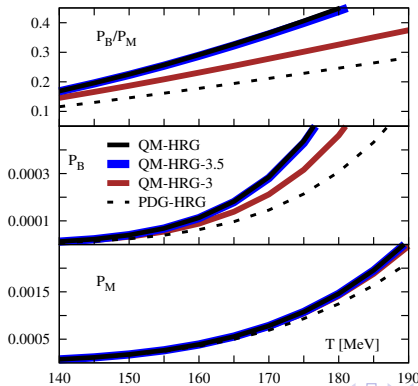
Charm hadron spectrum...story about missing states

- The charm meson sector is measured experimentally to quite good precision.
- Many charm baryons states not measured yet predicted from lattice and quark models [Ebert et. al, 10, Padmanath et. al., 13]
- Even spin-parity of ground state Λ_c not measured!



Relevance for QCD thermodynamics

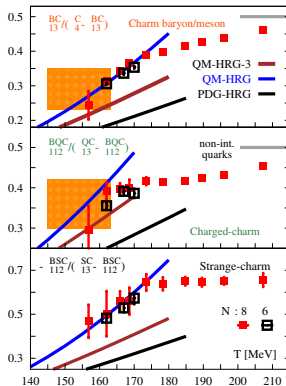
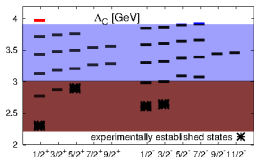
- We construct hadron resonance gas model with **experimentally known states: PDG-HRG**
- Compare with HRG with experimental+additional states: **QM-HRG**
- The partial pressure of mesons are similar
- In the baryon sector the difference starts showing up near T_c [Bielefeld-BNL collaboration, 14]



Our results

- Our methodology allows us to look at charm baryon sector exclusively
- Also look into the specific quantum number channels

- all hadrons: $\frac{p_B}{p_M} = \frac{\chi_{13}^{BC}}{\chi_4^C - \chi_{13}^{BC}}$
- S=1,2 hadrons: $\frac{\chi_{112}^{BSC}}{\chi_{13}^{SC} - \chi_{112}^{BSC}}$
- Q=1,2 hadrons: $\frac{\chi_{112}^{BQC}}{\chi_{13}^{QC} - \chi_{112}^{BQC}}$



QCD data seems to support the contribution of these additional baryon states to thermodynamics near T_c . [Bielefeld-BNL collaboration, 14]

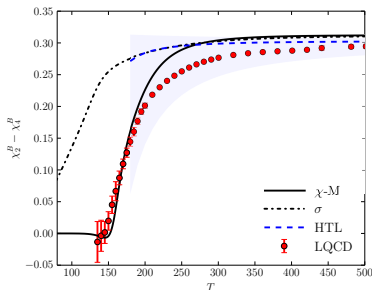
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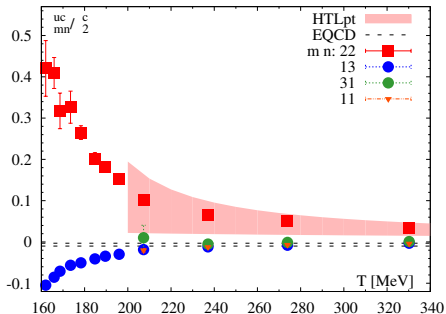
Non-perturbative nature of the QCD medium

- Above T_c , deconfinement of the color degrees of freedom occur.
- However the nature and/or existence of quasi-particles not well known for $T < 2T_c \Rightarrow$ any new insight to lattice data is clearly important.
- Matrix model for $SU_c(3)$ with non-trivial Polyakov loop potential could explain some of the essential features of **strongly coupled** pure gauge theory above T_d [Y. Hidaka and R. D. Pisarski, 08,09]
- Extension to chiral matrix model [R. D. Pisarski and V. Skokov, to appear] by adding 2+1 f quarks coupled to a meson nonet of both parities through Yukawa coupling + Potential for scalar fields symmetric under $SU(3)_L \times SU(3)_R \times Z(3)_A$ to mimic QCD.

- $\chi_2^B - \chi_4^B = 0$ in hadron phase, non-zero values signal deconfinement of quasi-particles carrying fractional B . [BI-BNL collaboration, 13]
- The Chiral Matrix model predictions for $\chi_2^B - \chi_4^B$ [R. D. Pisarski and V. Skokov, to appear] seems to agree with the continuum extrapolated lattice data [Budapest-Wuppertal collaboration, 14] for $T_c < T < 2T_c$.
- The Hard thermal loop perturbation theory agreement with lattice data only for $\sim 3 T_c$.
- Naive quark-meson model do not capture the physics \Rightarrow non-trivial eigenvalues or holonomy of the Polyakov loop seems to play a significant role for $T < 2T_c$.

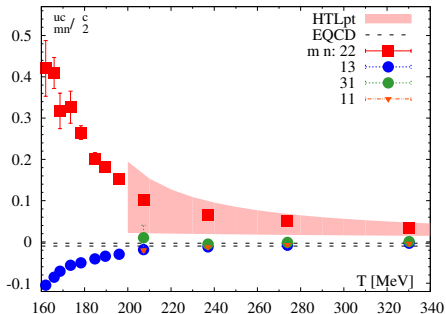


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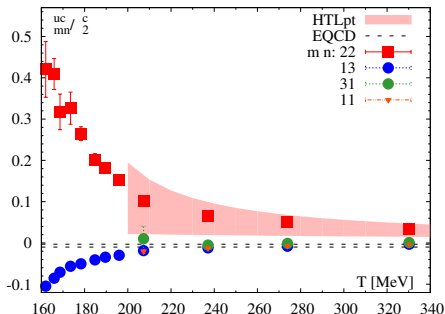
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- Hadrons melt but may survive as broad excitations till $1.2T_c$.
- Pressure for broad “quasi-particles” considerably lower than small width QP [Biro & Jakovac, 14]

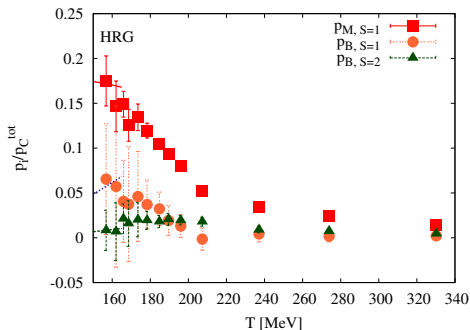
Degrees of freedom beyond T_c ?

- We look specifically at the sector of strange and charm hadrons where S and C quantum numbers are correlated only in the hadron phase.
- Upto 4th order derivatives additionally one has 3 more measurements $\chi_{[112]}^{BSC}$ apart from χ_{n+m}^{SC} and

$$p_{SC}(T, \mu_B, \mu_C, \mu_C) = \sum_{j=0}^1 p_{B,S=j}(T) \cosh\left(\frac{\mu_C + \mu_B - j\mu_S}{T}\right) + \\ p_M(T) \cosh\left(\frac{\mu_C + \mu_S}{T}\right) + (p_D(T)?).$$

- $p_D = \chi_{[211]}^{BSC} - \chi_{[112]}^{BSC} = 0$ for our data. Di-quarks carry color quantum number... should disappear when quark d.o.f start dominating.

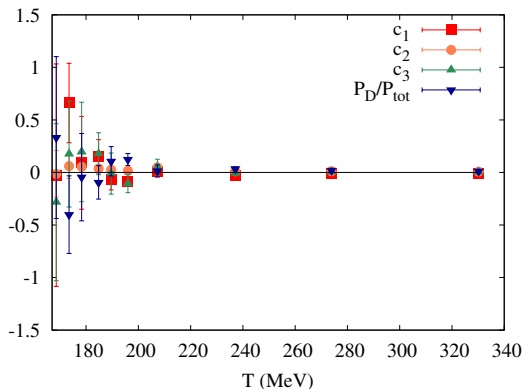
Degrees of freedom beyond T_c ?



- Meson and baryon like excitations survive upto $1.2 T_c$.
- Quark-quasiparticles start dominating the pressure beyond $T \gtrsim 200$ MeV \Rightarrow hints of strongly coupled QGP [S. Mukherjee, P. Petreczky, SS, 15].
- Strange baryon-like excitations suppressed than meson-like excitations.
- These studies consistent with screening mass of sc-mesons [Y. Maezawa et. al., 15].

Degrees of freedom beyond T_c ?

- For these calculations to be valid one should satisfy constraint relations \rightarrow smoothly connect to HRG and free gas at low and high T .



- Lattice data agree with the constraints imposed by our proposed model [S.Mukherjee, P. Petreczky, SS, 15].

What we learnt till now

- For many fluctuation related observables the prediction from a hadron Resonance gas already breaks down at $T \sim 140\text{-}145$ MeV.
- We took the lattice data and tried to constraint the experimental freezeout curve assuming thermalization. The result for freezeout $T_f = 147$ MeV at small baryon density consistent with expectation $T_f < T_c$.
- For heavy quarks we observe that charm baryons too melt near T_c .
- Additional charm baryons and resonances will contribute to thermodynamics near T_c .
- A similar contribution of these additional strange baryons and excitations \Rightarrow allows for a reduction of T_f by $5 - 8$ MeV [Bielefeld-BNL collaboration, 14]
contrary to the flavour hierarchy picture at T_c .

Perspectives

- The QCD medium at $T > T_c$ is non-perturbative, non-trivial holonomy plays a role in explaining the fluctuation data.
- For the charm sector, we observe baryon and meson like excitations surviving in the medium till $1.2 T_c$.
- Open charm hadrons melt at $T_c \Rightarrow$ freezeout temperature for D_s is now well known
Input for heavy flavour transport models [A. Beraudo et. al., 12]
- Additional baryons may contribute to hadronic interactions near the freezeout \rightarrow can it explain the discrepancy for between flow and suppression for D mesons?
- Our study more in favour for resonant scattering of heavy quarks in the medium [M. He, R. J. Fries, R. Rapp, 12].